

# LOAN DOCUMENT

		PHOTOGRAPH THIS SHEET <div style="border: 1px solid black; width: 100px; height: 80px; margin: 0 auto;"></div> <p style="text-align: center;">LEVEL</p>	PHOTOGRAPH THIS SHEET <div style="border: 1px solid black; width: 100px; height: 80px; margin: 0 auto; text-align: center;">           (5)         </div> <p style="text-align: center;">INVENTORY</p>																														
DTIC ACCESSION NUMBER	The Silicon Oscillating Accelerometer. . . . DOCUMENT IDENTIFICATION 1998																																
	<b>DISTRIBUTION STATEMENT A</b> Approved for Public Release Distribution Unlimited																																
	DISTRIBUTION STATEMENT																																
<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td colspan="2" style="text-align: center;">ACCESSION FOR</td> </tr> <tr> <td style="width: 50%;">NTIS</td> <td style="width: 50%;">GRAM <input type="checkbox"/></td> </tr> <tr> <td>DTIC</td> <td>TRAC <input type="checkbox"/></td> </tr> <tr> <td colspan="2">UNANNOUNCED</td> </tr> <tr> <td colspan="2">JUSTIFICATION</td> </tr> <tr><td colspan="2"> </td></tr> <tr><td colspan="2"> </td></tr> <tr><td colspan="2"> </td></tr> <tr><td colspan="2"> </td></tr> <tr><td colspan="2"> </td></tr> <tr> <td colspan="2">BY</td> </tr> <tr> <td colspan="2">DISTRIBUTION/</td> </tr> <tr> <td colspan="2">AVAILABILITY CODES</td> </tr> <tr> <td style="width: 50%;">DISTRIBUTION</td> <td style="width: 50%;">AVAILABILITY AND/OR SPECIAL</td> </tr> <tr> <td style="height: 40px; vertical-align: middle; text-align: center;">A-1</td> <td></td> </tr> </table> <p style="text-align: center;">DISTRIBUTION STAMP</p>		ACCESSION FOR		NTIS	GRAM <input type="checkbox"/>	DTIC	TRAC <input type="checkbox"/>	UNANNOUNCED		JUSTIFICATION												BY		DISTRIBUTION/		AVAILABILITY CODES		DISTRIBUTION	AVAILABILITY AND/OR SPECIAL	A-1		<div style="border: 1px solid black; width: 100%; height: 150px; margin-bottom: 10px;"></div> <p style="text-align: center;">DATE ACCESSIONED</p> <div style="border: 1px solid black; width: 100%; height: 100px; margin-bottom: 10px;"></div> <p style="text-align: center;">DATE RETURNED</p> <div style="border: 1px solid black; width: 100%; height: 100px;"></div> <p style="text-align: center;">REGISTERED OR CERTIFIED NUMBER</p>	
ACCESSION FOR																																	
NTIS	GRAM <input type="checkbox"/>																																
DTIC	TRAC <input type="checkbox"/>																																
UNANNOUNCED																																	
JUSTIFICATION																																	
BY																																	
DISTRIBUTION/																																	
AVAILABILITY CODES																																	
DISTRIBUTION	AVAILABILITY AND/OR SPECIAL																																
A-1																																	
<div style="border: 1px solid black; width: 100%; height: 80px; display: flex; align-items: center; justify-content: center; font-size: 2em;">         20010201 041       </div> <p style="text-align: center;">DATE RECEIVED IN DTIC</p>																																	
PHOTOGRAPH THIS SHEET AND RETURN TO DTIC-FDAC																																	

HANDLE WITH CARE

# THE SILICON OSCILLATING ACCELEROMETER: A MEMS INERTIAL INSTRUMENT FOR STRATEGIC MISSILE GUIDANCE

by

R. Hopkins, J. Borenstein, B. Antkowiak, P. Ward,  
R. Elliott, M. Weinberg, M. DePiero, J. Miola  
The Charles Stark Draper Laboratory, Inc.

## Abstract

The intercontinental ballistic missile (ICBM) and submarine-launched ballistic missiles (SLBM) developed over the past 50 years have employed successive generations of increasingly accurate inertial guidance systems. The comparatively short time of guided flight and high acceleration levels characteristic of the ballistic missile application place a premium on accelerometer performance to achieve desired weapon system accuracy. To date, the accelerometer design of choice for strategic missiles has been the Pendulous Integrating Gyroscopic Accelerometer (PIGA) instrument, an accelerometer whose origins trace back to the German V2 rocket, and has been refined through several generations of development to achieve unsurpassed performance. The specialized technologies of PIGA accelerometers, such as gas bearing wheels, ultra-stable ball bearings, precision electromagnetic components, and "designer chemical" flotation fluids require a costly support infrastructure for production and system life-cycle maintenance.

The Draper Laboratory is currently in the process of developing the Silicon Oscillating Accelerometer (SOA) a MEMS-based sensor that has the potential to achieve the ppm/ $\mu$ g performance stability required of the strategic missile application. The Microelectromechanical System (MEMS) technology is inherently low cost and offers a rapidly expanding commercial business base to leverage and sustain accelerometer production and deployment in next generation guidance systems.

The SOA belongs to the generic category of accelerometers known as Vibrating Beam Accelerometers (VBA), which sense acceleration by measuring the change in the resonant frequency of beam oscillators under the inertial loading of a proof mass. The SOA differs from conventional VBAs in one important respect; namely, the SOA is a silicon MEMS-based device, while VBAs, are typically bulk-fabricated quartz devices.

The silicon MEMS process offers several advantages over quartz that enable superior

accelerometer design features: 1) semiconductor grade single crystal silicon is a perfectly elastic structural material that can be produced with extremely low levels of impurities, 2) the MEMS process enables fabrication of very small (millimeter scale in the case of the SOA) resonator elements that are well isolated from the influence of parasitic instrument package stresses, and 3) capacitively based, electrostatic resonator actuation and sensing that offers greater design flexibility than the piezoelectric quartz technology.

This paper will give an overview of the Draper Lab SOA and current performance data taken to date.

## Introduction

### SOA Applications and Performance Goals

The ICBM/SLBM strategic missile has the most demanding requirements of any inertial guidance application. The high degree of accuracy required, combined with the high acceleration levels and large velocity at reentry body deployment place an especially stringent performance requirement on the guidance system accelerometers.

Though there are many system-derived performance parameters specified for inertial grade accelerometers (see Table 1), in broad terms, accelerometer performance can be characterized with two parameters: bias and scale factor (SF) stability. Accelerometer bias is the DC offset indicated from the instrument output under zero applied acceleration. Scale factor is the instrument gain or sensitivity that relates the applied acceleration to the instrument output signal (e.g., V/g, Hz/g, etc.).

To date, strategic grade performance has been achieved over the ICBM/SLBM mission times and hostile flight environments only in the PIGA, a highly refined instrument that has been employed successfully in U.S. strategic missile systems deployed since the inception of ICBM/SLBM programs. Unfortunately, the complexity of PIGA accelerometers (see Figure 1) and their specialized technologies, such as gas bearing wheels, ultra-stable ball bearings, precision electromagnetic components, and "designer chemical" flotation fluids require a costly support infrastructure for production and system life-cycle maintenance.

Table 1. SOA Performance Goals

Parameter	Units	Boost	Re-entry
• <b>Bias</b>			
- Repeatability	$\mu\text{g}$	1	100
- Stability	$\mu\text{g}$	1	5
-- Mission Time	min	17	60
• <b>Scale Factor</b>			
- Repeatability	ppm	1	100
- Stability	ppm	1	5
-- Mission Time	min	17	60
- Asymmetry	ppm	TBD	TBD
- $g^2$ (Compensated)	$\mu\text{g}/g^2$	0.1	0.2
- $g^3$ (Compensated)	$\mu\text{g}/g^3$	TBD	0.005
• <b>Resolution</b>	$\mu\text{g}/\sqrt{\text{Hz}}$	3	10
• <b>VRW</b>	ft/s/ $\sqrt{\text{h}}$	0.0042	0.014
• <b>Misalignment</b>			
- Repeatability	arcsec	0.1	5
- Stability	arcsec	0.1	2
• <b>Vibration Rect.</b>	$\mu\text{g}/(g\text{-rms})^2$	<0.15	<1
• <b>Bandwidth</b>	Hz	100	>100
• <b>Quantization</b>	ft/s/count	0.0001	0.001 -0.01
• <b>Max. Acceleration</b>	g	10	120

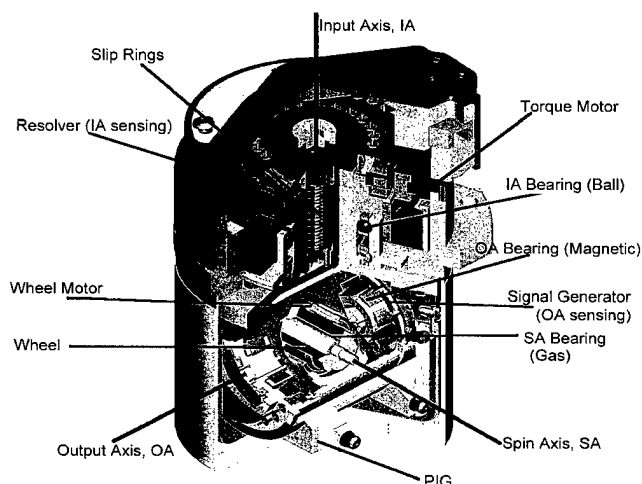


Figure 1. The 10 PIGA accelerometer.

Consequently, the strategic guidance community is seeking a lower cost, high reliability alternative to the PIGA for next generation ICBM/SLBM missile systems, with the important provision that performance remain uncompromised. Draper Laboratory is currently in the process of developing the SOA, a MEMS-based sensor that has the potential to achieve the ppm/ $\mu\text{g}$  performance stability required of the strategic missile application. The MEMS technology is inherently low cost and offers a rapidly expanding commercial business base to leverage and sustain accelerometer production and deployment in next generation guidance systems. The SOA belongs to the generic category of accelerometers

known as VBAs, which sense acceleration by measuring the change in the resonant frequency of beam oscillators under the inertial loading of a proof mass. The SOA differs from conventional VBAs in one important respect; namely, the SOA is a silicon MEMS-based device, while VBAs are typically bulk-fabricated quartz devices.

The silicon MEMS process offers several advantages over quartz that enable superior accelerometer design features: 1) semiconductor grade single crystal silicon is a perfectly elastic structural material that can be produced with extremely low levels of impurities, 2) the MEMS process enables fabrication of very small (millimeter scale in the case of the SOA) resonator elements that are well isolated from the influence of parasitic instrument package stresses, and 3) capacitively based, electrostatic resonator actuation and sensing that offers greater design flexibility than the piezoelectric quartz technology.

In addition to the above design advantages, the small size inherent to MEMS sensors enables the development of a compact IMU for reentry body (RB) instrumentation. Table 1 shows a comparison of accelerometer performance specifications typical of strategic boost-only and reentry instrumentation requirements. Note that the performance requirements specified for reentry are five to ten times more relaxed than the boost phase requirements.

The next sections describe the operational principles of the SOA, the MEMS fabrication process, and some SOA performance data.

### SOA Functional Description

The SOA developed by Draper Laboratory is a miniature silicon VBA fabricated using the silicon MEMS micromachining technology. Figure 2 is a schematic representation of the SOA sensor, showing a pair of double ended tuning fork oscillators connected to a common proof mass. These elements form a monolithic silicon structure that is supported above, and anodically bonded to a glass substrate as shown.

The SOA input axis lies in plane as indicated in Figure 2; under acceleration, the proof mass axially loads the two resonator pairs. The vibration frequency of each resonator changes under the applied load. This frequency change is measured and serves as the indicated acceleration output of the SOA. Note that the resonators are arranged so they are loaded differentially by the proof mass. That is, one resonator is placed in tension, the other in compression. This differential design doubles the sensitivity or scale factor of the accelerometer and furnishes a cancellation of error sources common to both resonators.

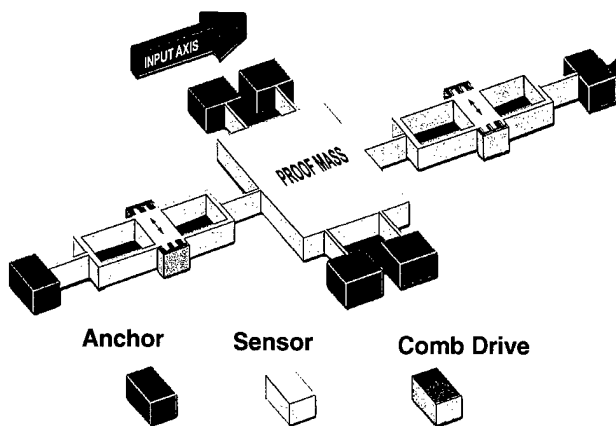


Figure 2. SOA schematic.

The resonators are excited by an electrostatic comb drive,<sup>[1],[2]</sup> similar to that used in Draper's micromechanical tuning fork gyro (TFG). The comb drive has both inner and outer motor stator combs that are fixed to the glass substrate. The outer motor combs apply the drive force, the inner motor combs sense the drive amplitude and frequency. A detail of the comb geometry is shown in Figure 3.

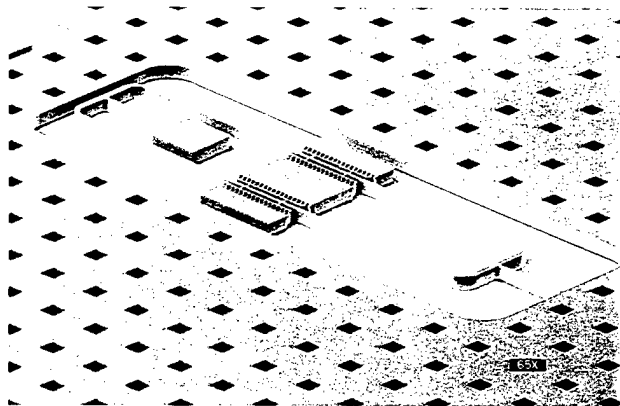


Figure 3. SOA oscillator detail.

The goal of the SOA design is to achieve a high SF, high Q resonator to meet the 1-μg/1-ppm strategic grade performance requirements. Large SF is desirable because it decreases the degree of frequency stability required to resolve a given acceleration level. For example, 0.1-mHz frequency stability is required of a 100-Hz/g SF unit to resolve 1 μg. A 10-Hz/g unit has a ten times more restrictive

frequency stability requirement (10 μHz) to resolve the same 1-μg input.

It can be shown<sup>[3]</sup> that the lateral stiffness of an axially loaded beam with fixed ends is:

$$K = \frac{12EI}{L^3} + \frac{12P}{\pi^2 L} \quad [1]$$

where: K = stiffness  
E = Young's modulus  
I = moment of inertia  
L = beam length  
P = axial load

If a lumped mass is supported between two beams, the natural frequency of the mass-beam system as a function of axial load is given by:

$$f = \sqrt{\frac{2}{m} \sqrt{\frac{12EI}{L^3} + \frac{12P}{\pi^2 L}}} \quad [2]$$

where: f = resonant frequency  
m = mass of lumped oscillator

Rearranging Eq. [2] gives:

$$f = f_o \sqrt{1 + \frac{L^2}{\pi^2 EI} P} \quad [3]$$

where: f = resonant frequency  
f<sub>o</sub> = nominal unloaded (bias) resonant

$$\text{frequency} = \sqrt{\frac{24EI}{mL^3}}$$

m = resonator mass  
L = beam length  
E = Young's modulus  
I = beam inertia  
P = applied axial load

Note that the frequency versus applied acceleration load relationship in the SOA is nonlinear, as indicated by Eq. [3] and shown in Figure 4.

A series expansion of Eq. [3] can be used to determine the linearized SOA SF (the slope about zero acceleration in Figure 4) and higher order g-coefficients:

$$f = f_o \left[ 1 + \frac{1}{2}SP - \frac{1}{8}S^2P^2 + \frac{1}{16}S^3P^3 - \dots \right] \quad [4]$$

where: S = L<sup>2</sup>/π<sup>2</sup>EI

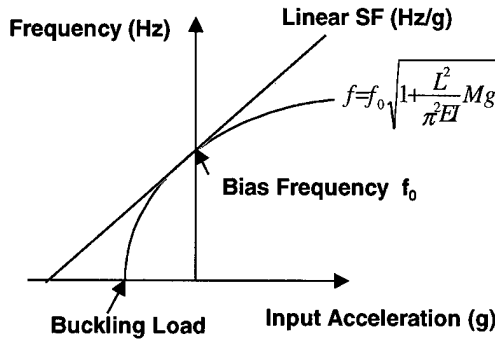


Figure 4. SOA frequency vs acceleration curve.

Equation [4] can be rewritten as:

$$f = f_0 + K_1 g + K_2 g^2 + K_3 g^3 - \dots \quad [5]$$

where:  $K_n = K_1 b_n (K_1/f_0)^{n-1}$  (Hz/g<sup>n</sup>)  
 $b_n = b_{n-1} (3-2n)/n$   
 $K_1 = f_0$  (S/2)  
 $b_1 = 1$   
 $g$  = acceleration

Note that the values of the  $g^2$  and  $g^3$  coefficients ( $K_2$ ,  $K_3$ ) are controlled by the linear SF ( $K_1$ ) and bias frequency ( $f_0$ ). The linearized SF is dependent on resonator dimensions, Young's modulus, and the mass of the resonator ( $m$ ) and proof mass ( $M$ ):

$$K_1 = \frac{M}{8\pi} \sqrt{\frac{L}{EI m}} \quad [6]$$

The SF stability of the SOA will be largely controlled by the Young's modulus sensitivity to temperature ( $\Delta E/E/\Delta T = -50$  ppm/ $^{\circ}$ C), as it is an order of magnitude larger than silicon's TCE (2.5 ppm/ $^{\circ}$ C), the parameter that would control the resonator dimensional stability. Given the square root relationship, the linear SF temperature coefficient is approximately 25 ppm/ $^{\circ}$ C, indicating that 0.01 $^{\circ}$ C temperature control will maintain better than 1-ppm SF performance.

From Eqs. [4] and [5], the values of the  $g^2$  and  $g^3$  coefficients ( $K_2$ ,  $K_3$ ) can be expressed by the linear SF ( $K_1$ ) and bias frequency ( $f_0$ ):

$$K_2 = -\frac{1}{2} \frac{K_1^2}{f_0} \quad [7]$$

$$K_3 = \frac{1}{2} \frac{K_1^3}{f_0^2} \quad [8]$$

For a 100-Hz/g (per side) SF, 20-kHz nominal bias frequency unit, Eqs. [7] and [8] project  $g^2$  and  $g^3$  coefficients of 0.25 Hz/g<sup>2</sup> and 0.0125 Hz/g<sup>3</sup>. Normalizing these coefficients by dividing by the linear SF gives 2500  $\mu$ g/g<sup>2</sup> and 12.5  $\mu$ g/g<sup>3</sup>, respectively.

Compensating these coefficients to the sub- $\mu$ g level is feasible because their stability will be of the order of the linear SF and bias. Differentiation of Eqs. [7] and [8] gives:

$$\frac{\Delta K_2}{K_2} = 2 \frac{\Delta SF}{SF} - \frac{\Delta f_0}{f_0} \quad [9]$$

$$\frac{\Delta K_3}{K_3} = 3 \frac{\Delta SF}{SF} - 2 \frac{\Delta f_0}{f_0} \quad [10]$$

Note that 1- $\mu$ g performance implies a resonator frequency stability ( $\Delta f/f$ ) on the order of 5 ppb (given a 100-Hz/g per side SF and 20-kHz nominal frequency unit). Combined with the 1-ppm SF requirement, this implies that the above SF nonlinearity coefficients should be stable to approximately 2 to 3 ppm. This high degree of stability should enable compensating the raw nonlinear coefficients to sub- $\mu$ g levels (although measuring the higher order  $g$ -coefficients will require careful centrifuge testing). Additionally, the net SOA  $g^2$  coefficient and other even order terms will be reduced as the  $g^2$  contribution from each resonator will be common mode differenced in the net SOA output.

### SOA Electronics

Figure 5 shows the SOA electronics block diagram. As mentioned above, the SOA employs an electrostatic comb drive to excite the resonators and to pick off the resonator displacement.

The magnitude of the drive force is given by:

$$F = \frac{1}{2} \frac{dC}{dx} V^2 \quad [11]$$

where:  $F$  = drive force  
 $dC/dx$  = comb position sensitivity  
 $V$  = applied voltage

The drive amplitude stability furnished by the electronics is critical to maintaining nominal resonator frequency stability. The resonator beams stiffen with lateral deflection, causing a dependence of the resonant frequency with drive amplitude. This nonlinear stiffening effect introduces a bias uncertainty from the resonator drive amplitude instability.

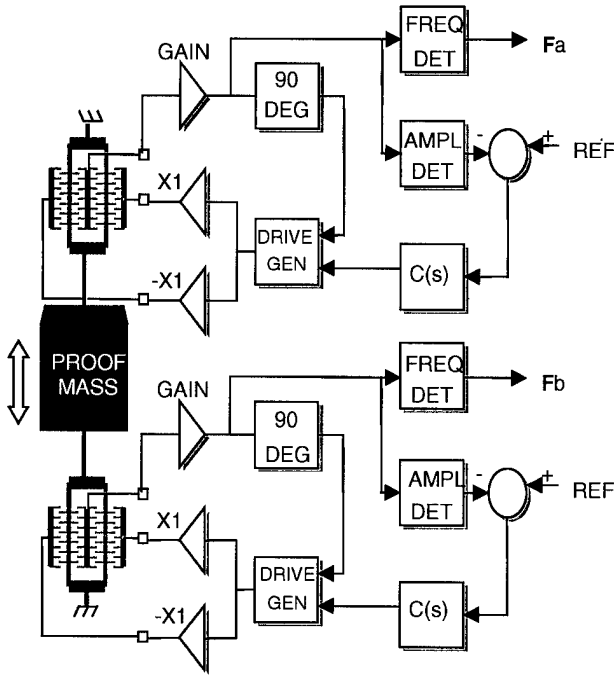


Figure 5. SOA electronics block diagram.

It can be shown<sup>[4]</sup> that if the resonator is modeled as a linear plus cubic stiffness element, the resonator frequency dependence on amplitude is given by:

$$f = f_o \left[ 1 + \frac{3}{8} \frac{K_3}{K} x^2 \right] \quad [12]$$

where:  $f$  = frequency at amplitude  $x$   
 $f_o$  = nominal resonant frequency  
 $K$  = linear stiffness of resonator  
 $K_3$  = cubic stiffness coefficient  
 $x$  = drive amplitude

The stability requirement on the drive amplitude can be determined by differentiating Eq. [12] to get:

$$\frac{\Delta f}{f_o} = \frac{3}{4} \frac{K_3}{K} x^2 \frac{\Delta x}{x} \quad [13]$$

From Eqs. [12] and [13] it can be seen that a small drive amplitude will minimize the resonator frequency variance from drive amplitude instability and noise. An alternate means of maximizing frequency

stability is to minimize the amount of nonlinear stiffening, i.e., design a resonator with a low  $K_3$  coefficient.

The resolution or noise floor of the SOA can be estimated by calculating the amplitude and phase noise associated with the sense comb frequency readout. From Reference [1], the capacitance

across a set of engaged comb drive fingers is given by:

$$C = 2 N \alpha \epsilon_o \frac{t}{g} L \quad [14]$$

where:  $C$  = capacitance  
 $\epsilon_o$  = permittivity of air  
 $N$  = number of teeth per side  
 $\alpha$  = fringing factor  
 $t$  = comb finger thickness  
 $g$  = air gap between fingers  
 $L$  = engaged length of fingers

The capacitance sensitivity to position (i.e., engaged length) is given by:

$$\frac{dC}{dx} = 2 N \alpha \epsilon_o \frac{t}{g} \quad [15]$$

where:  $dC/dx$  = sensitivity to position

Equation [12] gives the relationship between resonator amplitude and frequency, which gives the resonator frequency power spectral density (PSD) as:

$$\phi_f = f_o \frac{3 K_3}{4 K} x \phi_A \quad [16]$$

where:  $\phi_f$  = frequency PSD in Hz/ $\sqrt{\text{Hz}}$   
 $x$  = nominal drive amplitude  
 $\phi_A$  = amplitude noise PSD  
 $f_o$  = nominal resonant frequency  
 $K_3/K$  = stiffness coefficient ratio

The contribution of phase noise in the drive frequency electronics can also be estimated. The PSD of the oscillator phase noise is approximately equal to the PSD of the amplitude noise divided by the peak amplitude.

At resonance, the phase noise is related to frequency noise by:

$$\phi_f = \phi_p \frac{d\omega}{d\phi} = \phi_p \frac{\omega_n}{2Q} \quad [17]$$

where:  $\phi_f$  = frequency noise PSD  
 $\phi_p$  = phase noise PSD  
 $\omega_n$  = nominal resonant frequency  
 $Q$  = Q of resonator

The high Qs achieved in the SOA oscillators (~100,000) significantly reduce the frequency noise in the output from phase jitter. The net frequency noise in the SOA

readout is dominated by oscillator amplitude noise. Consequently, frequency readout resolution is improved with increasing bias voltage and decreasing drive amplitude.

### SOA MEMS Fabrication

For micromachining inertial instruments, Draper Laboratory employs the silicon-on-glass bulk dissolved-wafer process. The main process steps are illustrated in Figure 6. This process has been used in other inertial sensor fabrication. First, mesas are etched in the silicon wafer to form the gap between the suspended structures and the substrate. This process is done using potassium hydroxide, with a silicon dioxide etch mask. Once the  $\text{SiO}_2$  etch mask is removed, the silicon wafers undergo boron diffusion to form the etch stop layer; device thickness is determined by the depth of the boron diffusion. The device structural layer is then photolithographically patterned on the silicon, and wafers are etched using high-aspect-ratio micromachining in an Inductively-Coupled Plasma (ICP) machine. Wafers are then anodically bonded to glass substrates that have been metallized with the SOA electrode pattern. Finally, the silicon wafer is dissolved in an anisotropic wet etchant such as Ethylenediamine Pyrocatechol (EDP), to remove all but the heavily-boron-doped layer of silicon.

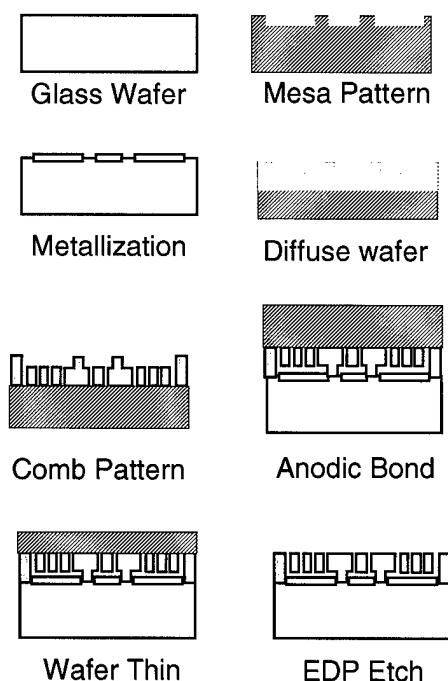


Figure 6. SOA fabrication process.

A scanning electron micrograph of the SOA oscillator flexure and oscillator mass is shown in Figure 7; the structure thickness is 12  $\mu\text{m}$ . Data from the

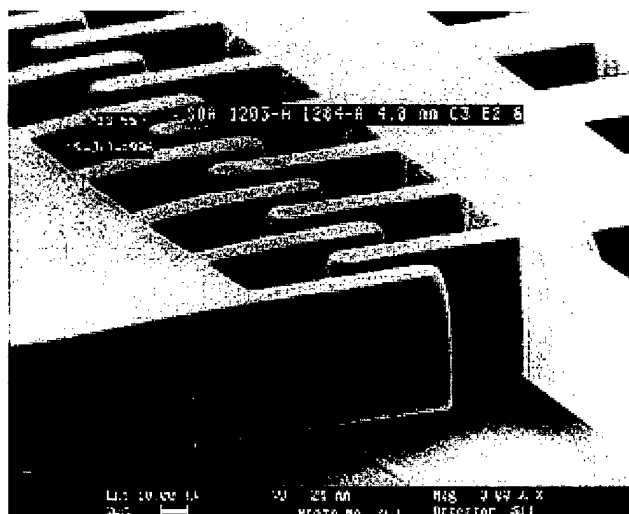


Figure 7. SOA oscillator detail.

SEM showed that the initial SOA oscillator flexure widths were, on average, three tenths of a micron larger than designed. This oversize can be corrected during fabrication of future devices, but test data contained here are for devices of this slightly wider flexure width.

### SOA Fabrication Screening

The first phase in assessing the viability of newly fabricated SOAs is to individually test the two SOA oscillators in air at a probe station. SOA test articles fabricated with a 3.5-, 4.0- and 4.5- $\mu\text{m}$  flexure width were used to confirm that the in-phase oscillator drive mode (i.e., the "Hula" mode) frequency is at least 10% lower than the out-of-phase drive mode for a wide range of beam geometry fabrication variation. A separation of at least 10% between the drive mode and the parasitic hula mode is desired to ensure that the hula mode does not interfere with the oscillator drive loop.

After probe testing, SOAs with satisfactory performance are packaged and integrated with preamplifier electronics. The SOA sensor is vacuum sealed in an aluminum oxide leadless ceramic chip carrier (LCCC), which is in turn bonded to a preamplifier alumina substrate for interfacing to breadboard electronics. The residual pressure achieved in the LCCC after vacuum seal is less than 1 mTorr, which ensures high oscillator Q factors. A plot of Q vs pressure for a typical SOA is shown in Figure 8.

### SOA Performance Test Data

Figure 9 shows an Allan Variance or Green's chart plot of an SOA. The standard deviation of indicated acceleration indicating SOA uncertainty is plotted against data averaging time. Note that the slope of the curve in the initial short averaging time periods is minus one half on a

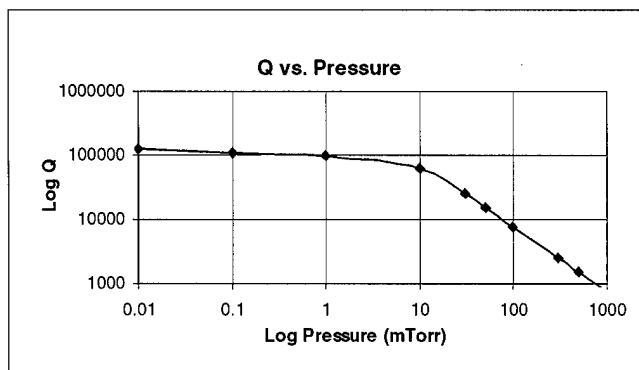


Figure 8. Q vs pressure relationship.

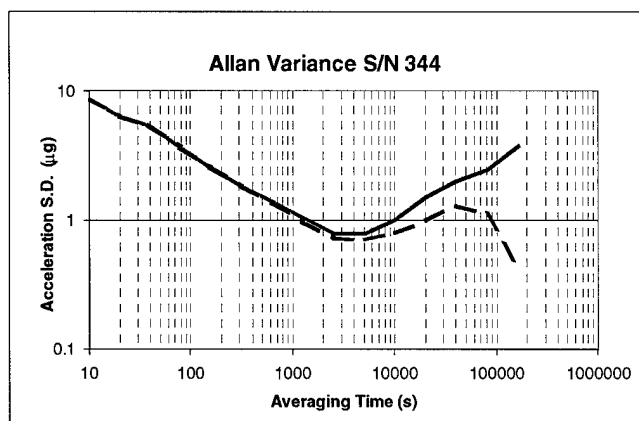


Figure 9. SOA Allan variance.

log scale, characteristic of instrument white noise. The equivalent white noise PSD can be calculated from a point on the minus one half slope line from:

$$\sigma^2 = \frac{2\phi}{T} \quad [18]$$

where:  $\sigma$  = acceleration standard deviation  
 $\phi$  = white noise PSD  
 $T$  = averaging time

The data from Figure 9 in the white noise region indicates, from Eq. [18], a white noise PSD of 23  $\mu\text{g}/\sqrt{\text{Hz}}$ . The equivalent velocity random walk coefficient is 0.031 ft/s/ $\sqrt{\text{h}}$ .

Note from Figure 9, that the SOA acceleration uncertainty drops below 1  $\mu\text{g}$  over averaging times that extend over approximately 1000 s. The region between approximately 2000 s and 10,000 s represents the "bucket" of the SOA where minimum instrument uncertainty is achieved over this data averaging period. For longer periods of time, uncertainty starts to increase, representing long-term drift and instability in the instrument. Note that Figure 9 shows two data curves, which are initially coincident,

but begin to diverge at longer averaging times. The solid curve that increases monotonically after 10,000 s is raw, uncompensated SOA output. The dashed curve was developed by applying a long-term drift compensation model to the SOA output.

Figures 10 and 11 show SOA bias and SF uncertainty. The data shown in these figures are 5-min (600-s) averaged data and are uncompensated SOA output. The data shown extend over a roughly 20-h period and show standard deviations in SF and bias of 3 ppm and 5  $\mu\text{g}$ , respectively.

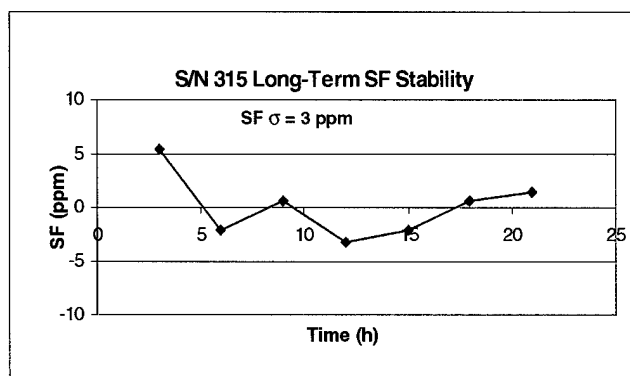


Figure 10. SOA scale factor stability.

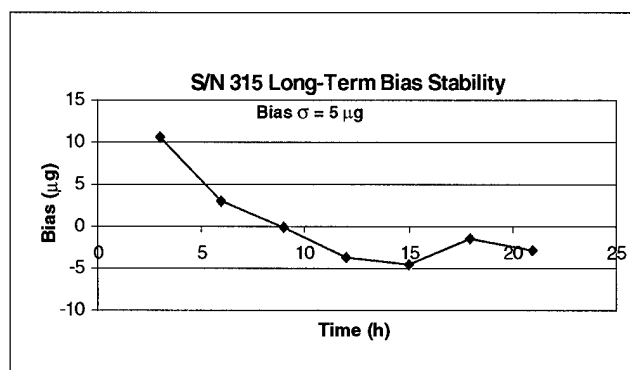


Figure 11. SOA bias stability.

## Conclusions

Draper Laboratory is currently in the process of developing the SOA, a MEMS-based inertial grade sensor. Performance data acquired to date approaches the levels needed for strategic guidance missions, both for traditional boost phase only guidance, and an emerging generation of reentry phase instrumentation applications.

The MEMS technology is inherently low cost and offers a rapidly expanding commercial business base to leverage and sustain accelerometer production and deployment in next generation guidance systems.



## **References**

- [1] Tang, William, *Electrostatic Comb Drive for Resonant Sensor and Actuator Applications*, Ph.D. Dissertation, University of California at Berkeley, 21 November 1990.
- [2] Kourepenis, A., J. Borenstein, J. Connelly, R. Elliott, P. Ward, M. Weinberg, "Performance of MEMS Inertial Sensors," 24<sup>th</sup> Joint Services Data Exchange for Guidance, Navigation, and Control, November 16-20, 1998, Anaheim, CA.
- [3] Roark and Young, *Formulas for Stress and Strain 5<sup>th</sup> Edition*, McGraw Hill, 1975.
- [4] Nayfeh, Mook, *Nonlinear Oscillations*, Wiley & Sons, New York, 1979.

## Government Disclosure Authorization Form

Disclosure authorization is required for all presentations. If this form is not received prior to the meeting the presentation will be canceled.

## PART I

Name of Author(s) R. HOPKINS, J. BORENSTEIN, B. ANIKOWITZ, R. WARD  
R. RELLITT, M. WEINBERG, M. ORRICO, J. MURPHY

Title of Paper: THE SILICON OSCILLATING TELECOMMUNICATOR: A MEMO  
INTERNAL INSTRUMENT FOR STRATEGIC MISSILE GUIDANCE

Classification of Paper/Presentation (circle one) SECRET CONFIDENTIAL UNCLASSIFIED

Author's Signature: R. E. Hopkins

\*\*\*\*\*

## PART II RELEASING OFFICIAL

Name of Releasing Official: Philip Young

Title: Document Control Supervisor

Address: 555 Technology Sq.

Cambridge, MA 02139

Telephone Number: (617) 258-3708

The Releasing Office, with the understanding that all attendees have current security clearances and that all attendees have approved need-to-know certification, and that no foreign national will be present, confirms that the overall classification of this paper is \_\_\_\_\_ and authorizes disclosure at the meeting.

Classified by: \_\_\_\_\_

Declassify on: \_\_\_\_\_

Distribution Statement: This is an Unclassified Technical Paper  
w/ no contract related material

Releasing Official's Signature: [Signature]



# PUBLICATION/VIDEO AND WEB AUTHORIZATION

For External Distribution and Formal Program Presentations

Media Services Job. No.

Doc./Video No. Assigned

P-3801

## A. DESCRIPTION - Please fill out completely

- Title of Document/Video: THE SILICON OSCILLATING ACCELEROMETER: A MEMS INERTIAL INSTRUMENT FOR STRATEGIC MISSILE GUIDANCE
- Author(s): HOPKINS, BORNSTEIN, ANIKOWIAK, WARD, JELLIOTT, WEINBERG, DEPIERO, MIDLA
- Charge Account No. 13049 OE GBIS Information generated under Account No. 13049
- Distribution:

☐ List included in document

☐ List attached

☒ List to be supplied by R. HOPKINS

Program

Internal Draper

TIC/Library

External

Total

No. of Copies

1

Return masters to: R. HOPKINS

- Will any invention be disclosed that has not been submitted to Draper's Patent Committee? ☐ Yes ☒ No

- Is sponsor review required for technical content? ☐ Yes ☒ No Sponsor: \_\_\_\_\_

### Public Dissemination:

To be published by: AIAA

Society/Organization: AIAA

Publication deadline date: 10/20/00

Name of meeting: MISSILE SCIENCES CONFERENCE

Meeting dates: 7-9 NOV. 2000 Location: MONTREY, CA

## B. EXTERNAL WEB SITE RELEASE - Needs to be filled out as completely as possible.

☐ NEW

☐ CHANGE

- Describe content of file(s): \_\_\_\_\_
- Where should the file be located on the Web Site? \_\_\_\_\_
- If external links are included, please describe the site(s) being linked to \_\_\_\_\_
- Who will be responsible for maintaining this material? \_\_\_\_\_
- Is there any copyrighted material included in this submission? ☐ Yes ☐ No If yes, then attach approval from copyright holder.

## C. APPROVAL SIGNATURES

Barbara Setherland  
Division Leader

Neil M. Barber

Date 10/18/00

Program Manager

Roy A. Litterick

Date 10/18/00

Education Director (Thesis ONLY)

[Signature]

Date

Contract Manager

[Signature]

Date 10/18/00

Security Director

[Signature]

Date 10/20/00

☒ N/A ☐ release as is ☐ review required

## D. REMARKS

\* R. Hopkins assured all pertinent info is in public domain (34)  
prior to release of paper, R. Hopkins must obtain clearance through  
Draper's Navy Program Office (W. O'Connor)

DOCUMENT CONTROL: Received \_\_\_\_\_ Copies from \_\_\_\_\_ Signed \_\_\_\_\_ Date \_\_\_\_\_

WEB SITE COMMITTEE MEMBER \_\_\_\_\_ Date \_\_\_\_\_

Posted on external Web Site by Network and Communications Services Date \_\_\_\_\_

WHITE-AUTHOR YELLOW-MEDIA SERVICES BLUE-CONTRACTS PINK-SECURITY OFFICE

AUTHOR



# Copyright Clearance and Assignment

## AIAA Technical Papers

Meeting AIAA MISSILE SCIENCES CONF.

Paper Number P-3801

Return to: AIAA Technical Papers Specialist  
1801 Alexander Bell Dr., Suite 500  
Reston, VA 20191-4344

You must sign each of the following:

- I. Clearance
- II. No-infringement statement
- III. Publication status
- IV. One copyright notice or assignment of release form only (A, B, C, or D)

Only one signature is required for joint works and guarantees that all authors agree to the terms set forth herein.

### I. CLEARANCE

This work is UNCLASSIFIED and has been cleared and approved for public release by the appropriate company and/or government agencies.

R. H. E. Hyl 10/18/00  
Signature of Author Date

### II. NO-INFRINGEMENT STATEMENT

Please make clear the copyright status of this work by signing the following affidavit assuring us that it contains no copyright-infringing material. This material represents original work by the author(s). No portion of the material is covered by a prior copyright; or for any portion copyrighted, the author has obtained permission for its use and all such permissions are in writing and attached to this form.

R. H. E. Hyl 10/18/00  
Signature of Author Date

### III. PUBLICATION STATUS

This work has not been published, nor is it currently under consideration for publication elsewhere.

R. H. E. Hyl 10/18/00  
Signature of Author Date

### IV. COPYRIGHT ASSIGNMENT

(Before signing, please read both sides of this form; NO VARIATIONS IN WORDING ARE ALLOWED.)

The copyright law effective 1 January 1978, gives the copyright of a work to the person who wrote it. AIAA prefers to hold the copyright of any work it publishes, with the clear understanding that the author and the author's organization have the right to reproduce it in print form (nonelectronic) for their own purposes, provided that the reproductions are not for sale. The Copyright Release Notice or Assignment of Release A does this.

Copyright Release Notice or Assignment of Release A: I assign copyright to my work to AIAA, giving the Institute all rights to it except that I and the organization by which I was employed at the time I wrote the manuscript have the right of further print reproductions, in part or in full, provided they are not for sale. This reproduction right does not include distribution of the work via the Internet or by other electronic means. [Note: If Copyright Release Notice or Assignment of Release A is signed, the copyright notice will read as follows: "Copyright (c) 20\_\_\_\_ by the American Institute of Aeronautics and Astronautics, Inc. All rights reserved."]

Signature of Author or Other Copyright Proprietor

Date

Occasionally, special situations arise in which the author (or his organization, if he has assigned his copyright to it) wishes to retain the copyright in his/her (or its) name. In such a case, AIAA requires a license to publish the work. The Copyright Release Notice or Assignment of Release B should be used for this purpose.

Copyright Release Notice or Assignment of Release B: I hereby license AIAA to publish this work and to use it for all of AIAA's current and future print and electronic uses. [Note: If the author retains Copyright Release Notice or Assignment of Release B, the copyright notice, in the name of the copyright holder, should appear at the bottom of the first page of the manuscript and should read as follows: "Copyright (c) 20\_\_\_\_ by \_\_\_\_\_. Published by the American Institute of Aeronautics and Astronautics, Inc., with permission."]

  
\_\_\_\_\_  
Signature of Author or Other Copyright Proprietor

10-27-00

\_\_\_\_\_  
Date

### TO AUTHORS EMPLOYED BY GOVERNMENT AGENCIES

1. A "work of the United States Government" (hereinafter called a Government work) is a work prepared by an officer or employee of the United States Government as part of that person's official duties. In some cases, works prepared by employees of private companies who are under contract to a Government agency may also be Government works.
2. Copyright protection under the U.S. Copyright Law is not available for any Government work; however, copyright protection is available for a work of a Government employee that is done apart from his or her official duties, and the copyright shall reside with the employee (subject to any transfer made by the employee).
3. When a work of a Government employee does not fall within the purview of his or her official duties, the employee's use of Governmental time, material, or facilities will not, of itself, make the work a Government work.
4. Under the current copyright law a work may be protected, within certain limitations, even if a copyright notice is not present; however, the presence of a copyright notice on a work makes it clear to a reader who the copyright proprietor is and who can grant a license to reproduce the work, etc.
5. If a work of a Government employee is not a Government work, AIAA will not publish the work unless AIAA receives an assignment (Copyright Release Notice or Assignment of Release A) or a license (Copyright Release Notice or Assignment of Release B).
6. Copyright Release Notice or Assignment of Release C is the appropriate assignment to be executed by a Government-employee author (except NASA employees) who has prepared a Government work.
7. Because of a master copyright agreement executed between NASA and AIAA, Copyright Release Notice or Assignment of Release D is the appropriate form for NASA-employed authors submitting Government works.
8. Please execute one of the four forms. If you are uncertain as to whether the work was outside your official duties, AIAA encourages you to seek appropriate counsel within your agency.

Copyright Release Notice or Assignment of Release C: This material is a work of the U.S. Government and is not subject to copyright protection in the United States. [Note: If Copyright Release Notice or Assignment of Release C is signed, the notice will read as follows: "This material is declared a work of the U.S. Government and is not subject to copyright protection in the United States."]

\_\_\_\_\_  
Signature of Author

\_\_\_\_\_  
Date

Copyright Release Notice or Assignment of Release D: I am employed by NASA and prepared this work as part of my official duties. [Note: If Copyright Release Notice or Assignment of Release D is signed, pursuant to the agreement between NASA and AIAA, the notice will read as follows: "Copyright (c) 20\_\_\_\_ by the American Institute of Aeronautics and Astronautics, Inc. No copyright is asserted in the United States under Title 17, U.S. Code. The U.S. Government has a royalty-free license to exercise all rights under the copyright claimed herein for Governmental purposes. All other rights are reserved by the copyright owner."]

\_\_\_\_\_  
Signature of Author

\_\_\_\_\_  
Date